Abstract—This paper investigates passivity-based pose control via an obstacle avoidance navigation function for three-dimensional (3-D) eye-in-hand visual feedback systems. Firstly, visual motion observer-based pose control for 3-D eye-in-hand visual feedback systems is presented. Next, a path planner to be appropriate for the visual motion error system is designed through an obstacle avoidance navigation function to keep collision-free during servoing. Finally, the effectiveness of the proposed method is verified through computer simulations.

I. INTRODUCTION

Visual feedback control is now a very flexible and useful method in robot control [1]. Recently, Allibert et al. [2] reported comparison results between two image prediction models for an image-based visual servoing scheme based on nonlinear model predictive control. Becerra et al. [3] presented a robust sliding mode control law that exploits epipolar geometries among three views. Zhang et al. [4] proposed a new 2-1/2-D visual servoing method for nonholonomic mobile robots based on a novel motion-estimation technique, which does not need homography/fundamental matrix estimation or decomposition. The authors have been proposed passivity-based visual feedback control for three-dimensional (3-D) target tracking in a series of papers [5]–[7].

Obstacle avoidance coupled with accurate path following control which is to move a vehicle towards a target location free of collisions with the obstacles has attracted much attention of a great amount of robotics researchers [8]. Huang et al. [9] proposed a local navigation method with a single camera for obstacle avoidance using headings to obstacles and their angular widths. Cherubini and Chaumette [10] presented appearance-based visual navigation with obstacle avoidance for real outdoor environments. This appearance-based visual navigation, which is one of the few methods for obstacle avoidance through the camera model, avoids new obstacles by using a range scanner. Although good vision-based navigation approaches for the obstacle avoidance problems are presented in [9] and [10], they are restricted to a ground vehicle.

On the other hand, in robot control, one of the representative works for obstacle avoidance problems is a method using a navigation function that is globally convergent potential function proposed by Rimon and Koditschek [11]. The feature of this efficient approach is that automatically merge path finding and trajectory generation in a closed-loop fashion. Some navigation function approaches for visual feedback systems are reported in [12]–[14]. Cowan et al. [12] proposed a visual feedback controller to bring a robot to rest at a desired configuration for an important problem that are all feature points remain within a camera field of view by using navigation functions. Chen et al. [13] and the authors [14] developed an off-line path planner based on an image space navigation function with an adaptive 2 1/2-D visual servoing controller and a stabilizing receding horizon one, respectively. However, all these approaches [12]–[14] take advantage of navigation functions to solve the camera field of view problems but not to deal with the obstacle avoidance problems.

In this paper, passivity-based pose control via a navigation function for obstacle avoidance is applied to 3-D visual feedback systems with an eye-in-hand configuration as shown in
Fig. 1. Firstly, passivity-based pose control for an eye-in-hand visual motion error system is proposed. Next, a path planner to be appropriate for the visual motion error system is designed through an obstacle avoidance navigation function in order to move the camera towards a desired pose and away from obstacles without additional sensors such as a range scanner. Convergence analysis of the proposed path planner is provided. Finally, we present simulation results that demonstrate the effectiveness of the proposed control scheme.

II. VISUAL MOTION OBSERVER-BASED POSE CONTROL

This section mainly reviews our previous work [5] via passivity-based visual feedback control with an eye-in-hand configuration.

A. Vision Camera Model

Visual feedback systems with an eye-in-hand configuration use three and $n$ coordinate frames which consist of a world frame $\Sigma_w$, a camera frame $\Sigma_c$, a target object frame $\Sigma_o$, and $n$ obstacle frames $\Sigma_{b1}, \cdots, \Sigma_{bn}$ as depicted in Fig. 1. Let $p_{co} \in \mathbb{R}^3$ and $e^{\hat{\theta}_{co}} \in SO(3)$ be a position vector and a rotation matrix from the camera frame $\Sigma_c$ to the object frame $\Sigma_o$. Then, a relative pose from $\Sigma_c$ to $\Sigma_o$ can be represented by $g_{co} = (p_{co}, e^{\hat{\theta}_{co}}) \in SE(3)$.

The objective of position-based visual feedback control is, in general, to bring the actual relative pose $g_{co}$ to a reference one $g_{cd}$. Firstly, we consider the relative pose $g_{co}$ in order to achieve the control objective. The relative pose from $\Sigma_c$ to $\Sigma_o$ can be led by using the composition rule for rigid body transformations as follows:

$$g_{co} = g_{wc}^{-1}g_{wo}. \quad (1)$$

The relative pose involves the velocity of each rigid body. To this aid, let us consider the velocity of a rigid body as described in [15]. We define the body velocity of the camera relative to the world frame $\Sigma_w$ as

$$\bar{v}_{wc} = [(v_{wc})^T (\omega_{wc})^T]^T,$$

where $v_{wc}$ and $\omega_{wc}$ represent the velocity of the origin and the angular velocity from $\Sigma_w$ to $\Sigma_c$, respectively [15].

Differentiating Eq. (1) with respect to time, the body velocity of the relative pose $g_{co}$ can be written as follows (See [5]):

$$v_{co}^b = -\text{Ad}_{(g_{co})}^{-1}v_{wc}^b + v_{wo}^b. \quad (2)$$

where $v_{co}^b$ is the body velocity of the target object relative to $\Sigma_w$ and $\text{Ad}_{(g_{co})}$ is the adjoint transformation associated with $g_{co} [15]$. The relative pose $g_{co} = (p_{co}, e^{\hat{\theta}_{co}})$ cannot be immediately obtained in the visual feedback system, because the target object velocity $v_{wo}^b$ is unknown and furthermore cannot be measured directly. To control the relative pose using visual information provided by computer vision system, we use the pinhole camera model with a perspective projection. Here, we consider $m(\geq 4)$ feature points on the rigid target object in this paper. Let $\lambda$ be a focal length, $p_{oi} \in \mathbb{R}^3$ and $p_{ci} \in \mathbb{R}^3$ be the position vectors of the target object’s $i$-th feature point relative to $\Sigma_o$ and $\Sigma_c$, respectively. Using a transformation of the coordinates, we have $p_{ci} = g_{co}p_{oi}$, where $p_{oi}$ and $p_{ci}$ should be regarded, with a slight abuse of notation, as $[p_{ci}^T]^T$ and $[p_{ci}^T]^T$ via the well-known homogeneous coordinate representation in robotics, respectively (see, e.g., [15]).

The perspective projection of the $i$-th feature point onto the image plane gives us the image plane coordinate $f_i := [f_{xi} f_{yi}]^T \in \mathbb{R}^2$ as

$$f_i = \frac{\lambda}{z_{ci}} \left[ \begin{array}{c} x_{ci} \\ y_{ci} \end{array} \right], \quad (3)$$

where $p_{ci} = [x_{ci} y_{ci} z_{ci}]^T$. It is straightforward to extend this model to $m$ image points by simply stacking the vectors of the image plane coordinate, i.e., $f(\hat{g}_{co}) := [f_1^T \cdots f_m^T]^T \in \mathbb{R}^{2m}$ and $p_c := [p_{c1}^T \cdots p_{cm}^T]^T \in \mathbb{R}^{3m}$. Hereafter, $f_{ab}$ means $f(\hat{g}_{ab})$ for simplicity. We assume that multiple point features on a known object are given and observed. Under this assumption, the image feature vector $f_{co}$ depends only on the relative pose $g_{co}$.

B. Estimation Error System

The visual feedback control task requires information of the relative pose $g_{co}$. Since the measurable information is only the image feature $f_{co}$ in the visual feedback system, we consider a nonlinear observer (we call a visual motion observer) in order to estimate the relative pose $g_{co}$ from the image feature $f_{co}$.

Firstly, using Eq. (2), we choose estimates $\hat{g}_{co}$ and $\hat{V}_{co}^b$ of the relative pose and velocity, respectively as

$$\hat{V}_{co}^b = -\text{Ad}_{(\hat{g}_{co})}^{-1}V_{wc}^b + u_e. \quad (4)$$

The new input $u_e$ is to be determined in order to drive the estimated values $\hat{g}_{co}$ and $\hat{V}_{co}^b$ to their actual values.

In order to establish the estimation error system, we define the estimation error between the estimated value $\hat{g}_{co}$ and the actual relative pose $g_{co}$ as

$$g_{ee} = \hat{g}_{co}^{-1}g_{co}. \quad (5)$$

We next define the error vector of the rotation matrix $e^{\hat{\theta}_{co}}$ as $r_{ci} := \text{sk}(e^{\hat{\theta}_{ci}})^T$ where $\text{sk}(e^{\hat{\theta}_{ci}})$ denotes $\frac{1}{2}(e^{\hat{\theta}_{ci}} - e^{-\hat{\theta}_{ci}})$. Using this notation, the vector of the estimation error is given by $e_e := [r_{ee}^T r_{ee}^T]^T$.

Suppose the attitude estimation error $\hat{\theta}_{ee}$ is small enough so that we can let $e^{\hat{\theta}_{ee}} \simeq I + \text{sk}(e^{\hat{\theta}_{ee}})$. Therefore, using a first-order Taylor expansion approximation, the estimation error vector $e_e$ can be obtained from image information $f_{co}$ and the estimated value of the relative pose $\hat{g}_{co}$ as follows:

$$e_e = J_e(\hat{g}_{co})(f_{co} - \hat{f}_{co}), \quad (6)$$

where $\hat{f}_{co}$ is the estimated value of image feature and $J_e(\hat{g}_{co})$ is an image Jacobian-like matrix [5]. In the same way as Eq. (2), the estimation error system can be represented by

$$\hat{v}_{ee}^b = -\text{Ad}_{(\hat{g}_{co})}^{-1}u_e + V_{wo}^b. \quad (7)$$
C. Pose Control Error System

Let us consider the dual of the estimation error system, which we call the pose control error system in order to achieve the control objective. Firstly, we define the pose control error as follows:

\[ g_{ec} = g_{cd}^{-1}g_{co}, \]  

which represents the error between the relative pose \( g_{co} \) and the reference one \( g_{cd} \). It should be remarked that \( g_{co} \) can be calculated by using the estimated relative pose \( \hat{g}_{co} \) and the estimation error vector \( e_c = [p_{ee}^T \ r_{ee}^T]^T \) equivalently as follows:

\[ g_{co} = \hat{g}_{co} g_{ec}, \]
\[ \xi\theta_{ee} = \frac{\sin^{-1}||r_{ee}||}{||r_{ee}||} r_{ee}, \]

although \( g_{co} \) cannot be measured directly. Similar to the estimation error vector, the vector of the pose control error is defined as \( e_c = [p_{ee}^T \ r_{ee}^T]^T \).

Differentiating Eq. (8) with respect to time, the pose control error system can be represented as

\[ V_{ec} = -Ad_{(g_{ec}^{-1})} \left( Ad_{(g_{cd}^{-1})} V_{wc}^b + V_{cd}^b \right) + V_{wo}^b, \]

where \( V_{cd}^b \) is the body velocity of the reference of the relative pose \( g_{cd} \).

D. Visual Motion Observer-based Pose Control

Combining the estimation error system (7) and the pose control one (11), we construct the visual motion observer-based pose control error system (we call the visual motion error system) as follows:

\[ \begin{bmatrix} V_{ec}^b \\ V_{be}^b \end{bmatrix} = \begin{bmatrix} -Ad_{(g_{ec}^{-1})} & 0 \\ 0 & -Ad_{(g_{cd}^{-1})} \end{bmatrix} u + \begin{bmatrix} I \\ I \end{bmatrix} V_{wo}^b, \]

where

\[ u := \begin{bmatrix} u_v^T \\ u_r^T \end{bmatrix}^T, \quad u_c := Ad_{(g_{ec}^{-1})} V_{wc}^b + V_{cd}^b. \]

Let us define the error vector of the visual motion error system as \( x := [e_c^T \ e_{\theta}^T]^T \), which consists of the pose control error vector \( e_c \) and the estimation error vector \( e_{\theta} \). It should be noted that if the vectors of the pose control error and the estimation one are equal to zero, then the actual relative pose \( g_{ec} \) tends to the reference one \( g_{cd} \) when \( x \to 0 \).

It can be proved that the visual motion error system (12) is passive from the input \( u \) to the output \(-x\) by using the following positive definite function:

\[ V = E(g_{ec}) + E(g_{ee}), \]

where

\[ E(g_{ec}) := K_c := \text{diag}\{K_c, K_{\theta} \}, \] and \( K_c := \text{diag}\{k_{c1}, \cdots, k_{c6} \} \) and \( K_{\theta} := \text{diag}\{k_{\theta1}, \cdots, k_{\theta6} \} \) are the positive gain matrices of \( x, y \) and \( z \) axes of the translation and the rotation for the pose control error and the estimation one, respectively.

Theorem 1 (5) If \( V_{wo}^b = 0 \), then the equilibrium point \( x = 0 \) for the closed-loop system (12) and (15) is asymptotic stable.

Theorem 1 shows Lyapunov stability for the closed-loop system. If the camera velocity \( V_{wc}^b \) is decided directly, the control objective is achieved by using the proposed control law (15).

III. OBSTACLE AVOIDANCE NAVIGATION

FUNCTION-BASED PATH PLANNING FOR EYE-IN-HAND SYSTEMS

Vision-based navigation with obstacle avoidance should offer great perspectives in many applications, such as surveillance, patrolling, search and rescue or high risk missions. In this section, as a first step for a vision-based navigation, we design a path planner through an obstacle avoidance navigation function for 3-D eye-in-hand visual feedback systems. The control objective in this paper is stated as follows:

Control Objective: The camera follows the target object, i.e., the relative pose \( g_{co}(t) \) is coincided with the time-varying desired one \( g_{cd}(t) \) which is generated to avoid unexpected obstacles, and which converges the final desired one \( g_{cdf} \).

From the proposed visual feedback control law, the input to the camera is designed as follows:

\[ V_{wc}^b = Ad_{(g_{cd})} (u_c - V_{cd}^b). \]

Hence, the camera input is needed the body velocity \( V_{cd}^b = [(\dot{\omega}_{cd}^b)^T \ (\omega_{cd}^b)^T]^T \) of the reference of the relative pose \( g_{cd} \).

A. Rotation Error for Path Planning

In rotation control, we consider only convergence to the final desired rotation. We define the rotation error between the time-varying relative desired rotation \( e_{\theta_{cd}} \) and the final one \( e_{\theta_{cdf}} \) as follows:

\[ e_{\theta_{cd}} = e^{-\xi_{\theta_{cdf}} e_{\theta_{cd}}}. \]

The vector form is defined as \( r_{cd} := sk(e_{\theta_{cd}}) \). Differentiating Eq. (17) with respect to time, the rotation error system for path planning can be written as

\[ \omega_{cd} = \omega_{cdf}. \]

B. Visual Motion Observer for Path Planning

Obstacle avoidance navigation function-based path planning needs the relative position of the obstacles from the camera frame \( p_{cb} \). In this section, we design the visual motion observer in order to estimate the relative position \( p_{cb} \), using the image feature \( f_{cb} := f(g_{cb}) \). Now, we assume that the multiple points on the obstacles can be observed and the

\[ \text{The relative pose } g_{cd} \text{ can be obtained solving } g_{cd} = g_{cd} g_{cdr}^{-1}. \]
position of them \( p_{hi} \) is known. The body velocity of the relative pose \( g_{cb} \) can be written as follows:

\[
V^b_{cb} = -\text{Ad}(g_{ch}^{-1}) V^b_{wc} + V^b_{ub},
\]

where \( V^b_{ub} \) is the \( i \)-th obstacle body velocity. Using the body velocity \( V^b_{cb} \), we establish a following estimate model for the obstacles:

\[
\bar{V}^b_{cb} = -\text{Ad}(\bar{g}_{cb})^{-1} V^b_{wc} + u_{hi},
\]

where \( \bar{g}_{cb} \) and \( \bar{V}^b_{cb} \) are the estimated values of \( g_{cb} \) and \( V^b_{cb} \), respectively. We define the estimation error \( e_{cb} \) between the actual relative pose \( g_{cb} \) and the estimated one \( \bar{g}_{cb} \) as follows:

\[
e_{cb} = J_e^e(\bar{g}_{cb})(f_{cb} - \bar{f}_{cb}).
\]

Hence, the relative position \( p_{cb} \) can be calculated as follows:

\[
p_{cb} = e^{-\hat{\phi}_{cb}} p_{cb} + \bar{p}_{cb}.
\]

through \( g_{cb} = \bar{g}_{cb} g_{cb} \). The estimation error system for the obstacles can be obtained as

\[
V^b_{cb} = -\text{Ad}(\bar{g}_{cb})^{-1} u_{hi} + V^b_{ub}.
\]

### C. Obstacle Avoidance Navigation Function

In this subsection, we develop the obstacle avoidance navigation function \( \varphi(p_{cd}) \) [11], [16]. In this paper, we assume that the workspace and the obstacles are spherical. This assumption does not constrain the generality of this work since it has been proven that navigation properties are invariant under diffeomorphisms in [16].

Firstly, we define a space \( D \) where the camera can move avoiding obstacles as follows:

\[
D = F - \bigcup_{i=1}^{M} B_i,
\]

where \( F := \{ p_{cd} : \| p_{cd} \| \leq \rho_0^2 \} \) is the camera movable space which represents a Euclidean 3-dimensional disk with the radius \( \rho_0 \geq 0 \), and \( B_i := \{ p_{cd} : \| p_{cd} - (p_{cd})_i \|^2 < \rho_i^2 \}, i = 1 \ldots M \) denotes a \( M \)-th obstacle space in \( F \) with the radius \( \rho_i > 0 \). We impose the additional constraint that all obstacles closures are contained in the interior of the workspace; i.e. \( \| p_{cd} - p_{cb} \| + \rho_i < \rho_0 \), \( 1 \leq i \leq M \), and that none of them intersect; i.e. \( \| p_{cd} - p_{cb} \| \geq \rho_i + \rho_j \), \( 1 \leq i, j \leq M \). If \( p_{cd} \in D \), the camera keeps collision-free.

The navigation functions used in this paper are defined as follows:

**Definition 1 ([11],[16]):** A smooth Morse function \( \varphi(p_{cd}) : D \rightarrow [0,1] \) is a navigation function if it is

1) a unique minimum exists at \( p_{cd} \);
2) uniformly maximal on the boundary of \( D \).

A smooth vector field on any sphere world with a unique attractor, must have at least as many saddles as obstacles. The property of a Morse function whose Hessian at all critical points is non-degenerate establishes that the initial conditions that bring the system to saddle points are sets of measure zero. In view of this property, all initial conditions away from sets of measure zero are brought to the unique minimum [16].

In order to design the obstacle avoidance navigation function, we utilize the following function which represents the error between the desired relative position \( p_{cd} \) and the final one \( p_{cdf} \):

\[
s(p_{cd}) = \| p_{cd} - p_{cdf} \|^{2\kappa},
\]

where \( \kappa > 0 \in \mathcal{R} \) is an additional parameter to change the potential field. Next, let define the obstacle function which includes the function \( \eta_0 \) for keeping in the space \( F \) as

\[
\eta(p_{cd}) = \sum_{i=0}^{M} \eta_i(p_{cd})
\]

\[
\eta_i(p_{cd}) = \begin{cases} \rho_i^2 - \| p_{cd} \|^2 & \text{for } i = 0 \\ \| p_{cd} - p_{cb} \|^2 - \rho_i^2 & \text{for } i = 1 \ldots M \end{cases}
\]

Then, the model space navigation function \( \hat{\varphi}(x) \in \mathcal{R}^{2m} \rightarrow [0,1] \) and a \( \kappa \)-th root function are defined as

\[
\hat{\varphi}(x) = \frac{x}{\mu + x}
\]

and

\[
\rho(x) = x^{\frac{1}{\kappa}},
\]

respectively, where \( \mu > 0 \in \mathcal{R} \) is a parameter. The function (29) is important in order to change \( p_{cdf} \) to a non-degenerate critical point. From Eqs. (26)–(29), the obstacle avoidance navigation function denoted by \( \varphi(p_{cd}) \in D \rightarrow \mathcal{R} \), can be developed as follows:

\[
\varphi(p_{cd}) = \rho \circ \hat{\varphi} \circ \frac{s(p_{cd})}{\eta(p_{cd})} = \left( \frac{s(p_{cd})}{\mu \eta(p_{cd}) + s(p_{cd})} \right)^{\frac{1}{\kappa}}
\]

where \( \circ \) denotes the composition operator. Using a similar way in [16], it can be verified that the function (30) is the navigation function if the parameter \( \kappa \) is selected adequately.

### D. Path Planning of Desired Body Velocity

We design the desired body velocity \( V^b_{cd} \) and the input for the estimation \( u_{hi} \) as follows:

\[
V^b_{cd} = \left[ -e^{-\xi \theta_{cd}} K_{dp} \nabla \varphi(p_{cd}) - K_{dr} e^{-\xi \theta_{cd}} T_{cd} \right]
\]

\[
u_{hi} = K_e e_{hi},
\]

where \( K_{dp} := \text{diag}(k_{dp1}, k_{dp2}, k_{dp3}) \), \( K_{dr} := \text{diag}(k_{dr1}, k_{dr2}, k_{dr3}) \) and \( K_e := \text{diag}(k_{e1}, \ldots, k_{e6}) \) are the positive gain matrices for the translation and the rotation of the desired body velocity and for the estimation input, respectively. \( \nabla \varphi(p_{cd}) := (\frac{\partial \varphi(p_{cd})}{\partial p_{cd}})^T \) which denotes
the gradient vector of $\varphi(p_{cd})$ can be calculated as Eq. (33) at the bottom of this page.

We state the main result of this paper concerning the convergence of the path planner.

**Theorem 2:** Suppose that $V_{\text{wc}} = 0$ and $V_{\text{wb}} = 0$, and the initial desired relative position $p_{cd}(0)$ satisfies $p_{cd}(0) \in D$. Then, the desired relative position $p_{cd}(t)$ ensures that $p_{cd}(t) \in D$ and $g_{cd}(t)$ has the asymptotically stable equilibrium point $g_{cd}$. \hfill $\blacksquare$

**Proof:** Consider the following positive definite function:

$$V_n = \varphi(p_{cd}) + \phi(e^{\xi_\theta_{cd}}) + \sum_{i=1}^{M} E(g_{ebi}). \quad (34)$$

Evaluating the time derivative of $V_n$ along the trajectories of Eqs. (18), (24), (31), (32) gives us

$$V_n = (\nabla \varphi)^T \dot{p}_{cd} + \varphi_{cd} \dot{e}^{\xi_\theta_{cd}} \omega \omega_{cd} + \sum_{i=1}^{M} e_{bi} \text{Ad}_{(e^{\xi_\theta_{bi}})} V_{ebi}$$

$$= (\nabla \varphi)^T \dot{e}^{\xi_\theta_{cd}} t_{cd} + \varphi_{cd} \dot{e}^{\xi_\theta_{cd}} \omega \omega_{cd} + \sum_{i=1}^{M} e_{bi} \text{Ad}_{(e^{\xi_\theta_{bi}})} \left(-\text{Ad}^{-1}_{(u_{bi})} u_{bi}\right)$$

$$= -(\nabla \varphi)^T e^{\varphi_{cd}} e^{-\varphi_{cd}} K_{dp} \nabla \varphi - \varphi_{cd} e^{-\varphi_{cd}} K_{dr} e^{-\varphi_{cd}} r_{cd} + \sum_{i=1}^{M} e_{bi} K_{ebi}$$

$$- \sum_{i=1}^{M} e_{bi} K_{ebi}. \quad (35)$$

It is clear from Eq. (35) that $V_n$ is a non-increasing function in the sense that

$$V_n \leq V_n(0). \quad (36)$$

From Eqs. (34) and (36), the condition $p_{cd}(t) \in D$, $\forall t > 0$ is satisfied for any initial condition $p_{cd}(0) \in D$. Since the estimation error vector $e_{bi} \rightarrow 0$, the position $p_{ebi}$ which is utilized in the obstacle functions converges actual value. Thanks to the property of navigation functions [16], it can be shown $p_{cd}(t) \rightarrow p_{cdf}$ through $\nabla \varphi(p_{cd}) \rightarrow 0$. On the other hand, the rotation $e^{\varphi_{cd}} \rightarrow e^{\varphi_{cdf}}$ can be verified because of $e^{-\varphi_{cdf}} r_{cd} \rightarrow 0$. Therefore, it can be concluded that $g_{cd}(t) \rightarrow g_{cd}$.

**Theorem 2** guarantees the convergence of the time-varying desired pose $g_{cd}(t)$ to the final one $g_{cdf}$. The path planner can be designed to keep collision-free based on the obstacle avoidance navigation function. The block diagram of the visual motion observer-based eye-in-hand pose control with the obstacle avoidance navigation function-based path planner is shown in Fig. 2.

\[ \nabla \varphi(p_{cd}) = \frac{2\mu}{\kappa(\mu \eta + s)^{\frac{1}{\kappa}}} \left( \kappa(p_{cd} - p_{cdf}) + \|p_{cd} - p_{cdf}\|^2 \right) \quad (33) \]

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**IV. Verification**

In this section, we present simulation results for the visual feedback control with the path planner via the obstacle avoidance function, compared with the constant desired relative pose proposed in [5]. The control objective is that the camera tracks the static target object to avoid two obstacles. In other words, it is bring the actual relative pose $g_{co}(t)$ to a given reference one $g_{cdf}$ using a time-varying reference $g_{cd}(t)$, and it can be achieved to make both the estimation and the pose control errors zero.

The simulation is carried out with the initial condition $p_{co} = [-1.25 4.994 0.5]^T$ m, $\theta_{co} = [0 0 -\pi/12]^T$ rad. The final desired relative pose is $p_{cdf} = [0 1.5 0]^T$ m, $\theta_{cdf} = [0 0 0]^T$ rad. The other conditions are set as $p_{cb1} = [-0.224 1.095 0]^T$ m, $\theta_{cb1} = [0 0 -\pi/12]^T$ rad, $p_{cb2} = [-1.414 2.45 0.75]^T$ m, $\theta_{cb2} = [0 0 -\pi/12]^T$ rad, $\rho_2 = 0.5$ m.

The simulation results are presented in Figs. 3 and 4. Fig. 3 shows the actual pose control error $e_r$, which is the error vector between the current relative pose $g_{co}(t)$ and the final desired one $g_{cdf}$. The asymptotic stability can be confirmed by steady state performance in Fig. 3.
This paper proposes passivity-based 3-D eye-in-hand visual feedback control via an obstacle avoidance navigation function. The main contribution of this paper is to show that the path planner which can avoid obstacles during servoing is designed for 3-D eye-in-hand visual feedback systems. Simulation results are presented to verify the control performance of the proposed control scheme with obstacle avoidance. Although only simulation results are shown in this submitted version, experimental movies using a Parrot AR.Drone which is a wifi quadrotor aerial vehicle with two cameras are available at http://www.kanazawa-it.ac.jp/kawai/research/ARDrone/ARDronemovies.html.

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